	Outline	
SOCIOLOGY UNVERSITY OF LIMERICE UL Summer School: Regression session 2 Brendan Halpin, Sociology 2023 Summer School	Session 2	Session 2 Outline
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 Outline Multiple regression: more than 1 explanatory variable Estimate net effects of each variable, controlling for the others Very important class of statistical model Begin by considering 3-way relationships in the abstract Then consider the mechanics of multiple regression 	Session 2 Multidimensional causality	 Multidimensional causality Regression analysis never proves causal relationships, but it "thinks" in causal terms To use it we need to understand causal relationships: what process generates the data we see, and what can regression tell us about it. Start by considering the relationship between variables and patterns of association
3-variable nictures	Correlated X variables	Snurious association
 Let's consider patterns of causality and association between three variables, X1 and X2, and Y If X1 and X2 are not correlated with each other, their separate effects on Y more or less just add up X1 Y	 But if X1 and X2 are correlated, things can get funny: X1	 X1 may have an association with Y, implying a causal relationship But if X2 affects both X1 and Y the relationship between X1 and Y may be spurious X1 // Y X2
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- Where there is a time-order (X1 before X2), we may see direct and indirect effects
- X1 may affect X2, which affects Y, but not affect Y directly
- Thus there is association between X1 and Y without a direct causal effect





Direct and indirect effects Suppression Interactions • Where X1 and X2 have positive effects on Y, but a negative correlation, or · An interaction effect is where the effect of one variable on Y changes different effects on Y with a positive correlation, the association between X1 depending on the value of another and Y may be supressed · However, it is possible for both direct and indirect effects to be present at the . That is, it may be invisible if we don't take account of X2 X1 ─── Y same time X1 — ⁺ → Y X2 X2 sociology 💥 sociology 💥 sociology 💥

	Multiple explanatory variables	Unpicking multiple effects
Session 2 Multiple regression	 Regression analysis can be extended to the case where there is more than one explanatory variable – multiple regression This allows us to estimate the net simultaneous effect of many variables, and thus to begin to disentangle more complex relationships Interpretation is relatively easy: each variable gets its own slope coefficient, standard error and significance The slope coefficient is the effect on the dependent variable of a 1 unit change in the explanatory variable, <i>while taking account of the other variables</i> 	 We will see how regression can be used to throw light on the 3-variable problems we have described above Over-estimation of X1's effect Spurious X1 X1 with an indirect (mediated) effect Under-estimation of X1's effect (suppression) X1's effect differing according to the values of X2 (interaction)
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Example: Over-estimation	Aside: Dichotomous variables	3-variable Logic
 Example: income may be affected by gender, and also by work hours: competing explanations – one or the other, or both could have effects 	 We deal with gender in a special way: this is a <i>binary</i> or <i>dichotomous</i> variable has two values 	
We can fit bivariate regressions:	• We turn it into a yes/no or 0/1 variable - e.g., female or not	
$\mathit{Income} = \mathit{a} + \mathit{b} imes \mathit{WorkTime}$	 If we put this in as an explanatory variable a one-unit change in the explanatory variable is the difference between being male and female 	• X1 (hours) is correlated with income (higher H, higher I)
or	• Thus the <i>c</i> coefficient we get in the	 X2 (gender) attects income (temales lower) Hours and gender are strongly associated (females lower)
Income = $a + b \times Female$	<i>income</i> = $a + b \times Work I me + c \times Female regression is the net change in predicted income of females, once you take account of work hours.$	
	The <i>b</i> coefficient is then the net effect of a unit change in work hours, once	
$income = a + b \times work nme + c \times remaie$	you take gender into account.	
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Regression: Just hours	Regression: Hours and binary gender	3-var logic
. reg Income Hours Source SS df MS Number of obs = 506 Model 86947928.8 1 86947928.8 Prob > F = 0.0000 Residual 570128215 504 1131206.78 R-squared = 0.1323 Adj R-squared = 0.1326 Total 657076144 506 1301140.88 Root MSE = 10036 Income Coef. Std. Err. t P>(t) [950 Cosf. Interval] Hours 37.82204 4.314061 8.77 0.000 29.34628 46.2978 449.7435 150.1722 2.99 0.003 154.703 744.7841	. reg Income Hours i.Gender Source SS df MS Number of obs = 506 Model 110236231 2 55118115.6 Prob 5 F = 0.0000 Residual 546339812 503 1087156.8 R-squared = 0.1678 Adj R-squared = 0.1645 Total 657076144 505 1301140.88 Root MSE = 1042.7 Income Coef. Std. Err. t P>(t) [05% Conf. Interval] Hours 28.33657 4.699451 6.03 0.000 19.1056 37.57155 Gender female -478.4214 103.3684 -4.63 0.000 -681.5084 -775.3344 _cons 1022.139 192.2717 5.32 0.000 644.3844 1399.893	 The gender gap reduces (but not to zero) if you control for hours The effect of hours controlling for gender falls
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Spurious relationship	Maths and height by regression	Spurious relationship: controlled for
 Sometimes controlling for X2 makes the effect of X1 entirely disappear X1 -> Y is a "spurious" relationship 	. reg maths height Source SS df MS Number of obs = 1,000 F(1,998) = 1706.40 F(1,998) = 1706.40 F(1,998) = 0.0000 Residual 138021.727 998 138.29324 R.equared = 0.6310 Adj R-squared = 0.6306 Total 374013.599 999 374.387887 Root MSE = 11.76 maths Coefficient Std. err. t P>tt [95% conf. interval] height 1.058213 .0256173 41.31 0.0000 1.007943 1.108483 _cons -89.11002 4.200327 -21.22 0.000 -97.3585 -80.87555	. reg maths height age Source SS df MS Number of obs = 1,000 F(2, 997) = 1273.62 Model 268802.74 2 134401.37 Prob F = 0.0800 Residual 105210.858 997 105.527441 R.aquared = 0.7181 Ad JB =anuared = 0.7181 Total 374013.599 999 374.387987 Root MSE = 10.273 maths Coefficient Std. err. t P> t [95% conf. interval] height0067167 .0644065 -0.10 0.9171331045 .1106711 age 9.579467 .5432093 17.63 0.000 8.513385 10.64555 cons -57.8381 4.074241 -14.21 0.000 -65.87888 -49.88874
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Regression controls for linear effects	Regression: Direct and indirect 1	Regression: Direct and indirect 2
 We have seen this spurious relationship debunked visually by separating into 6 year groups (subsetting the sample) Regression does it by attributing an effect to age Accounting for age strips the effect of height Regression can be more efficient than subsetting the sample if the effect is linear, additive. 	. reg ownscore fatherscore Source SS df MS Number of obs = 1,000 Model 13269.3853 1 13269.3853 Prob > F = 0.0000 Residual 247525.861 998 244.02100 Å Arequared = 0.0509 Total 260795.247 999 261.0566303 Root MSE = 15.749 ownscore Coef. Std. Err. t P>tt [95% Conf. Interval] fatherscore .237029 .032413 7.31 0.000 .4724773 .3006844 _cons 37.90661 1.672157 22.67 0.000 34.62726 41.18996	. reg education fatherscore Source SS df MS F(1, 992) = 1,000 Model 311.104929 1 311.104929 Prob > F = 0.0000 Residual 2777.00007 998 2.00261129 R-squared = 0.1001 Adj R-squared = 0.0092 Total 3108.111 999 3.1122222 Root MSE = 1.6741 education Coef. Std. Err. t P> t [95% Comf. Interval] fatherscore .0343018 .003456 10.54 0.000 .0295405 0.433031 _cons 1.295213 .1777516 7.29 0.000 .9464035 1.644023
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Regression: Direct and indirect 3	Regression: Direct and indirect 4	Interaction
<pre>. reg ownscore education Source SS df MS Mumber of obs = 1,000 F(1, 998) = 447.54 Model 80742.8091 1 80742.8091 Prob > F = 0.0000 Residual 180052.437 998 180.413264 R-agured = 0.3089 Adj R-agured = 0.3089 Total 280795.247 999 261.065303 Root MSE = 13.432 ownscore Coef. Std. Err. t P>ltl [95% Conf. Interval] education 5.096871 .2409273 21.16 0.000 4.624098 5.569653 _cons 33.87079 .8556481 39.58 0.000 32.19171 35.54988 </pre>	. reg ownscore education fatherscore $\frac{Source}{Source} = \frac{SS}{S} \frac{df}{S} \frac{MS}{F(2, 997)} = \frac{1,000}{F(2, 997)} = \frac{226.41}{226.41}$ Model 81453.7212 2 40726.8606 Frob > F = 0.0003 Residual 179341.525 997 179.851169 R-aquared = 0.3133 Adj R-aquared = 0.3139 Total 260795.247 999 261.056303 Root MSE = 1.3.412 ownscore Coef. Std. Err. t P> t [95% Conf. Interval] education 4.937369 .2535982 19.47 0.000 4.439722 5.435017 fatherscore 31.51367 1.461439 21.56 0.000 28.64582 34.38152	• Where the effect of X1 changes across values of X2, we have "interaction"
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$\begin{array}{c c c c c c c c c c c c c c c c c c c $. reg Income Hours if Gender==2 Source SS df MS Number of obs = 274 P(1, 272) = 42,63 Nodel 31772944.2 1 31772944.2 Prob > F = 0.0000 Residual 202744304 272 745383.469 R.sequared = 0.1355 Adj R.sequared = 0.1355 Adj R.sequared = 0.1353 Total 234517248 273 859037.537 Root MSE = 863.36 Income Coef. Std. Err. t P> t [95% Conf. Interval] Hours 29.70376 4.549594 6.53 0.000 20.74687 38.660055 come 504.6153 140.3614 3.660 0.000 228.2824 780.9462	. reg Income c.Hours##i.Gender Source S5 df MS Number of obs = 506 P(3, 502) = 33.82 Model 110486228 3 36628742.8 Prob > F = 0.0000 Residual 546589915 502 1088824.53 R. equared = 0.1651 Adj R.squared = 0.1652 Total 657076144 505 1301140.88 Root MSE = 1043.5 Income Coef. Std. Err. t P> t [95% Conf. Interval] Hours 24.61855 9.076915 2.71 0.007 6.785132 42.45198 Gender female -659.7502 392.3082 -1.68 0.093 -1430.518 111.0181 Gender#c.Hours 5.085207 10.61255 0.48 0.632 -15.78529 25.9357 cons 1164.366 353.7327 3.29 0.001 469.3865 1859.345
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